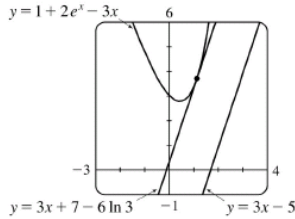


48. The slope of $y=1+2e^x-3x$ is given by $m=y' = 2e^x-3$.
 The slope of $3x-y=5 \Leftrightarrow y=3x-5$ is 3.

$m=3 \Rightarrow 2e^x-3=3 \Rightarrow e^x=3 \Rightarrow x=\ln 3$. This occurs at the point $(\ln 3, 7-3\ln 3) \approx (1.1, 3.7)$.



32. We are given that $f(3)=4$, $g(3)=2$, $f'(3)=-6$, and $g'(3)=5$.

(a) $(f+g)'(3) = f'(3) + g'(3) = -6 + 5 = -1$

(b) $(fg)'(3) = f(3)g'(3) + g(3)f'(3) = (4)(5) + (2)(-6) = 20 - 12 = 8$

(c) $\left(\frac{f}{g}\right)'(3) = \frac{g(3)f'(3) - f(3)g'(3)}{[g(3)]^2} = \frac{(2)(-6) - (4)(5)}{(2)^2} = \frac{-32}{4} = -8$

(d)

$$\begin{aligned} \left(\frac{f}{f-g}\right)'(3) &= \frac{[f(3)-g(3)]f'(3) - f(3)[f'(3)-g'(3)]}{[f(3)-g(3)]^2} \\ &= \frac{(4-2)(-6) - 4(-6-5)}{(4-2)^2} = \frac{-12+44}{2^2} = 8 \end{aligned}$$

40. (a) $f(20)=10,000$ means that when the price of the fabric is \$20/ yard, 10,000 yards will be sold.

$f'(20)=-350$ means that as the price of the fabric increases past \$20/ yard, the amount of fabric which will be sold is decreasing at a rate of 350 yards per (dollar per yard).

(b) $R(p)=pf(p) \Rightarrow R'(p)=pf'(p)+f(p) \cdot 1 \Rightarrow R'(20)=20f'(20)+f(20) \cdot 1 = 20(-350)+10,000=3000$. This means that as the price of the fabric increases past \$20/ yard, the total revenue is increasing at \$3000/(\$/yard). Note that the Product Rule indicates that we will lose \$7000/(\$/yard) due to selling less fabric, but that that loss is more than made up for by the additional revenue due to the increase in price.

10. $y = \frac{1+\sin x}{x+\cos x} \Rightarrow$

$$\begin{aligned} y' &= \frac{(x+\cos x)(\cos x) - (1+\sin x)(1-\sin x)}{(x+\cos x)^2} = \frac{x\cos x + \cos^2 x - (1-\sin^2 x)}{(x+\cos x)^2} \\ &= \frac{x\cos x + \cos^2 x - (\cos^2 x)}{(x+\cos x)^2} = \frac{x\cos x}{(x+\cos x)^2} \end{aligned}$$