

20. Suppose the month is February. Your payment on the 28th day would be $2^{28-1} = 2^{27} = 134,217,728$ cents, or \$1,342,177.28. Clearly, the second method of payment results in a larger amount for any month.

10. The graph of $f(x) = 1 + 4x - x^2$ is a parabola with axis of symmetry $x = -\frac{b}{2a} = -\frac{4}{2(-1)} = 2$. Pick any x -values equidistant from 2 to find two equal function values. For example, $f(1) = 4$ and $f(3) = 4$, so f is not 1-1.

$$22. m = \frac{m_0}{\sqrt{1 - v^2/c^2}} \Rightarrow 1 - \frac{v^2}{c^2} = \frac{m_0^2}{m^2} \Rightarrow \frac{v^2}{c^2} = 1 - \frac{m_0^2}{m^2} \Rightarrow v^2 = c^2 \left(1 - \frac{m_0^2}{m^2} \right) \Rightarrow v = c \sqrt{1 - \frac{m_0^2}{m^2}}. \text{ This}$$

formula gives us the speed v of the particle in terms of its mass m , that is, $v = f^{-1}(m)$.

26.

$$\lim_{x \rightarrow 0} \frac{x-1}{x^2(x+2)} = -\infty \text{ since } x^2 \rightarrow 0 \text{ as } x \rightarrow 0 \text{ and } \frac{x-1}{x^2(x+2)} < 0 \text{ for } 0 < x < 1 \text{ and for } -2 < x < 0.$$