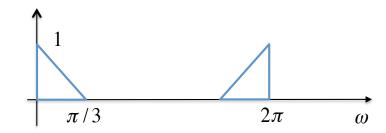
## $\mathbf{Hw2}$ Due Oct. 2, '14

## Answers without justifications will not be given credits

- 1. Let  $x(n) = 0.5(\delta(n-1) + \delta(n+1))$ .
  - (a) Determine  $X(e^{j\omega})$ . (Simplify the expression as much as possible)
  - (b) Plot  $X(e^{j\omega})$ .
  - (c) Plot  $|X(e^{j\omega})|$ .
  - (d) Plot  $\angle X(e^{j\omega})$ .
- 2. Let x(n) be real and  $X(e^{j\omega})$  be as plotted in the following figure.



- (a) Plot  $X(e^{j(\omega-\pi/4)})$ .
- (b) Let  $Y(e^{j\omega}) = 0.5(X(e^{j(\omega-\pi/4)}) + X(e^{j(\omega+\pi/4)}))$ . Determine y(n) in terms of x(n).
- 3. Let h(n) be the ideal lowpass filter with cut-off frequency  $\pi/4$ .
  - (a) Let the input of h(n) be  $x(n) = (-1)^n$  for all n. Determine the output of h(n).
  - (b) \* Consider the following system, where x(n) is as in (a). Determine y(n).

