$Hw1 {\rm ~Sept.~24,~'15}$

Answers without justifications will not be given credits

- 1. Consider the 5-point moving average system. Let the input x(n) = u(n).
 - (a) Compute and plot the output y(n).
 - (b) Is the system LTI? If so, identify the impulse response h(n).
 - (c) Is the system stable? Is it causal?
- 2. Suppose a system whose output y(n) is related to its input x(n) by

$$y(n) = \begin{cases} x(n/2), & \text{if } n \text{ is even} \\ 0, & \text{otherwise.} \end{cases}$$

Determine whether the system has one or more of the following properties.

- (a) linearity
- (b) time invariance
- (c) causality
- (d) stability
- 3. * Consider the following system.
 - (a) Express y(n) in terms of x(n) and h(n).
 - (b) Is the overall system from x(n) to y(n) LTI? Find the impulse response if it is.

$$x(n) \xrightarrow{w(n) = x(n)e^{j\pi n}} h(n) \xrightarrow{h(n)} y(n)$$

- 4. * MATLAB (optional, due next week in class) Let h(n) be a 3-pt moving average system.
 - (a) Let the input be x(n) = 1 for $n = 0, 1, \dots, 6$. Plot the output.
 - (b) Let the input be $x(n) = (-1)^n$ for all n. Plot the output y(n) for an appropriate range of n.
 - (c) Compute $H(e^{j\omega})$ for $\omega = \pi$ and use it to obtain the output y(n) in (b) by hand. Is the result the same as what you have in (b)?